DC MOTOR DRIVE CONTROL USING FUZZY PD+I CONTROLLER BASED GA TUNING

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ABSTRACT

This article presents a control method for DC motor drive using Fuzzy PD+I controller based Genetic Algorithm (GA). This control method is adequate whenever it is possible to apply a PID controller or this controller is already applied. The idea behind this controller is to adjust a conventional PID control parameters (K_p , K_i and K_d) using GA and then determine the equivalents of these gains in the fuzzy domain. The tuned controller parameters are used as initial values for parameters of the fuzzy PD+I controller. The proposed controller, fuzzy PD+I controller has the feature to be either linear or non-linear controller to obtain a better performance. Testing the proposed controller for the DC motor drive to control the speed of the motor over a wide range of the operating speed is applied. Moreover, the proposed fuzzy PD+I controller succeeds at improving the system performance even with changing the system parameters.

Keywords: *Fuzzy PD+I, scaling factors, DC motor drives, Speed Control.*

1. INTRODUCTION

The DC motor drives are still used in industrial applications where fine speed adjustment is needed. Different control techniques are used to control the speed of the DC drive. There are many methods of speed control of DC motors including field control, armature voltage control, and armature resistance control methods [1]. The most commonly used method of speed control is the armature voltage control thanks to the new developments in the power electronic devices [2]. These power electronic devices used for the speed control of DC motors based armature voltage are mainly electronic converter controllable rectifier or PWM chopper to supply a controllable voltage to the motor.

Consequently, there will be nonlinearity in the motor characteristics. Some new controllers have the ability to deal with the non-linearity in the systems, among them fuzzy logic controllers [3-6]. The performance of fuzzy logic controllers depends mainly on the control rules and the scaling factors. Hence, the optimization of these parameters has been one of the most investigated problems in the theory of fuzzy systems. In many of the fuzzy logic controllers proposed some optimization techniques are used for tuning the parameters [7]. PID controller is still used in abundance in industry as it is characterized by its simplicity structure and robust performance in a wide range of operating conditions. There are many methods for

tuning the parameters including Ziegler-Nichols, analytical methods, and evolutionary computing techniques like Genetic Algorithms (GA) and Particle Swarm Optimization (PSO), [8-10]. GA has many applications in electrical systems for optimization applications [8-9]. The fuzzy with certain assumptions has the same performance like PID controllers [4]. This paper presents robust DC motor drive for speed control using Fuzzy PD+I Controller based GA Tuning. GA is used for tuning the PID controller parameters by minimizing the integral sum of square of error (ISE) between the motor speed and a reference speed. Transferring the obtained optimized PID control into fuzzy PD+I controller by applying input and output scaling factors of the fuzzy PD+I controller to PID control parameters. To test the validity of the fuzzy PD+I through PID controllers at the linear state, no saturation in the system is assumed and the system should have the same response for the two controllers. Another tuning of the scaling factors of the equivalent linear fuzzy PD+I controller are performed to transform it into a nonlinear controller. This transformation from linear to nonlinear controller is due to the fact that the greater the nonlinearity variations, the greater the possibility of a high-performance controller [4]. To design a fuzzy PID controller, a three dimension rule base should be established. This enlarges the rule base and complicates the inference engine and the defuzzification process. For this reason, the rule base has a two-dimensional space, the error and the rate of change of error. The integral action is accomplished separately in the non-fuzzy domain in order to construct the rule base on a two-dimensional space instead of three. Introducing the non-fuzzy integral branch

has the advantage of simplifying the rule base without affecting the controller's overall performance. The DC motor drives are still used in industrial applications where fine speed adjustment is needed.

2. MATHEMATICAL MODEL OF THE DC MOTOR

The motor dynamics can be described in the following two equations:

$$\dot{i}_a = -\frac{R_a}{L_a}i_a - \frac{K}{L_a}\omega + \frac{1}{L_a}V_t \quad (1)$$

$$\dot{\omega} = \frac{K}{J_a}i_a - \frac{D}{J_a}\omega - \frac{1}{J_a}T_L \quad (2)$$

Where i_a , ω , V_t , R_a , L_a , J_a , K , D and T_L are the armature current, rotor speed, terminal voltage, armature resistance, armature inductance, rotor inertia, torque and back emf constant, damping constant and load torque respectively.

3. THE FUZZY LOGIC CONTROLLER

When a PID controller is already implemented, it is possible to make use of the known PID controller design before implementing the fuzzy controller. A systematic tuning procedure by carrying PID tuning rules over to the fuzzy domain is as follows:

- a. Tuning a PID controller
- b. Replacing it with an equivalent linear fuzzy controller
- c. Converting the linear fuzzy controller into a nonlinear one
- d. Fine tune it

3.1 TUNING A PID CONTROLLER USING GA

Genetic algorithms (GAs) are biologically inspired techniques used for optimization. This algorithm encode a potential solution to a specific problem on a simple chromosome like data structure and apply

recombination operators to these structures so as to preserve critical information [11-13]. The GA begins with defining the optimization variables, the fitness function, and the fitness. It ends by testing for convergence or with the maximum generations. In this paper, the goal of optimization is to find the PID controller parameters that minimize the ISE of the objective function, J , defined in (3). The cost function, J , is given by:

$$ISE(K_p, K_i, K_d) = \frac{1}{t} \int_0^t (N_{ref} - N_{mot})^2 dt \quad (3)$$

Where N_{ref} and N_{mot} are the reference and motor speeds respectively. In GAs, all of the possible values of the PID control parameters are coded in chromosomes. Series binary coding is used in this work. Next a fitness function (ISE) is calculated with initial value of the controller parameters, to compare the chromosomes which have to be defined. Therefore, to calculate the fitness of a chromosome, the optimization function has to be calculated using the information in the chromosome. Finally the optimization process stopped if the minimum value of fitness function is reached or maximum number of generations is reached [10-12]. The flow chart of GA used for PID controller tuning is given in Figure 1.

Fig. 1. Genetic Algorithm flowchart for PI Controller Tuning.

The overall system using PID controller is depicted in Figure 2.

Fig. 2. Overall system using a PID controller

3.2 LINEAR FUZZY CONTROLLER

The second step is to replace the summation in PID control by a linear fuzzy controller acting like a summation. The closed loop system should thus show exactly the same step response. The following checklist summarizes the general design choices for achieving a fuzzy rule base equivalent to a summation (see Appendix A):

- Use triangular input sets that cross at $\mu = 0.5$
- Use algebraic product for *and* connective.
- The rule base must be the outer *and* product of all input families.
- Use output singletons, positions determined by the sum of peak positions of the input sets.

In order to minimize the size of the rule base, the integral action is separated and performed in the non-fuzzy domain as shown in Figure 3. The integral error is computed as:

$$ie_n = \sum_{i=1}^n (e_i \times T_s) \quad (4)$$

Fig. 3. Fuzzy PD+I controller

The rule base that contains nine rules is used in this paper are given in Table 1.

TABLE 1 NINE RULES USED IN THIS PAPER.

$\begin{matrix} ce \\ e \end{matrix}$	Neg	Zero	Pos
Neg	NB	NM	ZE
Zero	NM	ZE	PM
Pos	ZE	PM	PB

The membership functions for the input and output variables are shown in Figures 4 and 5 respectively.

Fig. 4. Membership functions for the inputs error and change of error

Fig. 5. Membership functions for the singleton output

The controller is thus a function of the three inputs e , ce , and ie as in equation (5)

$$U_n = [f(G_E \times e_n, G_{CE} \times ce_n) + G_{IE} \times ie_n] \times G_U \quad (5)$$

Its linear approximation is

$$\begin{aligned} U_n &= [G_E \times e_n + G_{CE} \times ce_n + G_{IE} \times ie_n] \times G_U \\ &= G_U G_E e_n + G_U G_{CE} \times ce_n + G_U G_{IE} \times ie_n \end{aligned} \quad (6)$$

Comparing (3) and (6), the gains are related in the following way:

$$K_p = G_U \times G_E \quad (7)$$

$$K_d = G_U \times G_{CE} \quad (8)$$

$$K_i = G_U \times G_{IE} \quad (9)$$

There is one degree of freedom, so, G_E is adjusted first according to the universe of discourse to exploit the range fully, and then the other parameters can be computed easily.

3.3 MAKING THE FUZZY CONTROLLER NONLINEAR

The third step in the design procedure is to make the fuzzy controller nonlinear. The shape of the sets and the choice of rules affect the control strategy and the dynamics of the closed loop system [4]. It is difficult to make a fair and objective comparison of their control characteristics. One should select a type of surface that fits the problem at hand. It is recommended to start a design procedure with the linear surface and tune the gains and then replace it with a nonlinear surface that is suitable for the system under study.

3.4 FINE-TUNING THE FUZZY NONLINEAR CONTROLLER

The forth step is to fine-tune the gains by intuition and experience; if the sampling time is too short, the computation of ce_n will become too sensitive to noise. On the other hand, one would choose G_E as large as possible to cover the range of the universe exactly. However, an increase in G_{CE} will increase the derivative gain, so one would keep it as small as possible in order to keep noise problems to a minimum. The good choice of G_U is very important too. If it is so small, the response will be very slow, hence, one would select it as large as possible without creating too much overshoot. A procedure of hand-tuning a fuzzy PD+I controller is the following:

- Select a suitable value for G_E such that it exploits the range of the universe fully.
- Set $G_{IE} = G_{CE} = 0$
- Tune G_U to give the desired response, ignoring any final value offset.
- Increase the proportional gain G_U and adjust the derivative gain G_{CE} to dampen the overshoot.
- In order to remove any final value offset, adjust the integral gain G_{IE} .
- Repeat the procedure until G_U is as large as possible.

4. SIMULATION RESULTS

Numerical values of the parameters of the DC motor are as follows [5]:

$P = 5kW$	$V_t = 220V$	$N = 1500rpm$
$R_a = 0.5\Omega$	$L_a = 14mH$	$J_a = 0.15kg.m^2$

$K = 1.4$	$D = 0.01Nm.s.$
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Many case studies are selected in order to show the validity of the proposed controller and comparison through classical PID method tuned by GA. The simulation results shown in Figure 5 are carried out as follows: At ($t = 0$), the drive is assumed to operate at steady state with initial load torque corresponding to $0.5 p.u.$ At ($t = 1$ s) a step in the speed command amount to $0.1 p.u.$ is simulated, and at ($t = 2$ s) another step in the load torque corresponding to full load value is also simulated. Figure 6 shows the speed responses for steady state speeds of 1350, 750, and 250 rpm respectively. A separate case corresponding to initial steady state speed of 550 rpm is shown in Figure 7 in order to clarify the details of the response.

Fig. 6. The speed responses to $0.1 p.u.$ step in speed command with initial s.s. speeds of (A) 1350 rpm, (B) 750 rpm, and (C) 250 rpm.

Fig. 7. A separate simulation case with initial steady state speed of 550 rpm.

The results show that the proposed controller provides relatively fast and non-oscillatory speed response with small settling time. Only a dip in speed response results when changing the load torque from $0.5 p.u.$ to full load. Another test is taken as an example for the parameters variations of the system. This situation is a simulation in the case of increasing the inertia to double its value due to the added inertia of the load to that of the motor. Figure 8 shows the speed responses for steady state speeds of 1350, 750, and 250 rpm respectively with doubling the inertia. Also, a case corresponding to initial steady state speed of 550 rpm with double inertia is dropped out and is shown in Figure 9 for more details. It is shown that the proposed controller has modified its action as a result to this

parameters variation. This assures the robustness of the proposed controller.

Fig. 8. The responses to 0.1 p.u. step in speed command when the drive operates at double its normal inertia

Fig. 9. A separate simulation case with initial steady state speed of 550 rpm and double inertia

The output of the fuzzy controller as well as the integral controller output is shown in Figures 10 and 11 for the case with initial speed of 1350 rpm and rated inertia.

Fig. 10. The output of the fuzzy controller with initial speed of 1350 rpm

Fig. 11. The output of the integral controller and corresponding to initial s.s. speed of 1350 rpm.

It can be noted that the PD fuzzy controller plays its main role in transient periods, while it resets its output at the steady state periods leaving the separated integral controller to perform its mission. Also, the armature voltage and armature current curves are illustrated in Figure 12 and 13 for the case of 1350 rpm initial speed and rated inertia.

Fig. 12. The armature voltage response at steady state speed of 1350 rpm

Fig. 13. The armature current response at initial steady state speed of 1350 rpm

5. CONCLUSION

DC motor drive using Fuzzy PD+I controller is introduced in this paper to control the motor speed. Fine tuning of PID controller with GA is applied to minimize the ISE to obtain optimal PID control parameters. The optimal values for classical PID controller parameters obtained by GA are set to be the initial values for tuning PI+D fuzzy controller in the transformation of classical PID into Fuzzy PD+I controller. With some modification and rules applied, the proposed DC motor drive control can be operated in both non-linear and linear modes. Many cases are studied including the operation with different starting steady state speeds, changing the system parameters, and abrupt load change. Both the control voltage and the armature current responses ensure the healthy operation of the combined fuzzy PD+I controller. The obtained results show that the controller provides fast and non-oscillatory speed responses and it helps in paving the way to improve the performance of the existing analog controllers which are present in most of the process in industry.

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APPENDIX (A)

Assume both inputs, E and CE , are defined on a standard universe $[-100, 100]$ as shown in Figure (A-1)

Fig. A-1. Membership function for both E and CE

The sum of the membership values for each input is "1" which can be achieved when the sets are triangular and cross their neighbor sets at the membership value $\mu = 0.5$. Any input value can thus be a member of at most two sets and the membership of each is a linear function of the input value. The output sets should preferably be singletons s_i , since it simplifies the defuzzification. The rule base can be defined as in Table A.1.

TABLE A.1 THE RULE BASED

$E \backslash CE$	Pos	Neg
Pos	s_1	s_2
Neg	s_3	s_4

Referring to the rule base, the contribution to the control signal from the first rule is

$$\mu_1 \times s_1 = \mu_{Pos}(E) \wedge \mu_{Pos}(CE) \times s_1 \quad (A-1)$$

To ensure linearity, we must choose the algebraic product for the connective and, i.e.

$$\mu_1 \times s_1 = \mu_{Pos}(E) \times \mu_{Pos}(CE) \times s_1 \quad (A-2)$$

The combination of all contributions, using COA defuzzification is

$$u = \frac{\mu_1 \times s_1 + \mu_2 \times s_2 + \mu_3 \times s_3 + \mu_4 \times s_4}{\mu_1 + \mu_2 + \mu_3 + \mu_4} \quad (A-3)$$

To simplify the notation, we will substitute

$$\begin{aligned} x &= \mu_{Pos}(E), \quad 1-x = \mu_{Neg}(E) \\ y &= \mu_{Pos}(CE), \quad 1-y = \mu_{Neg}(CE) \end{aligned} \quad (A-4)$$

Notice that the denominator of (A-3) is

$$xy + x(1-y) + (1-x)y + (1-x)(1-y) \quad (A-5)$$

It is clear from (A-5) that the denominator of (A-3) is "1". This means that it doesn't affect the calculations. However, the numerator is completely different,

$$\begin{aligned} N(E, CE) &= \mu_1 \times s_1 + \mu_2 \times s_2 + \\ &\quad \mu_3 \times s_3 + \mu_4 \times s_4 \\ &= xys_1 + x(1-y)s_2 + \\ &\quad (1-x)ys_3 + (1-x)(1-y)s_4 \end{aligned} \quad (A-6)$$

Clearly $x, y \in [0,1]$ since they are really fuzzy membership functions, and (A-6) is simply a bilinear interpolation between the four scalars s_1, s_2, s_3 , and s_4 . Since x is a linear function in E and y is a linear function in CE , the numerator $N(E, CE)$, and thereby the controller output U_n , is a bilinear function in E and CE . When $(x,y) = (1,1)$, all other terms but the one holding s_1 are zero, and when $(x,y) = (1,0)$, all other terms but the one holding s_2 are zero, etc. Since $(x,y) = (1,1)$ when $(E, CE) = (100, 100)$, then s_1 should be chosen to be 200 in order to obtain the sought equivalence with the summation $E+CE$. The rest of the singletons should be chosen in a similar way, yielding

$$(s_1, s_2, s_3, s_4) = (200, 0, 0, -200)$$

What has been said can be generalized to input families with more than two input sets per input, because only two input sets will be active at a time.

By this way, we can obtain a linear control surface like this of Figure (A-2).

Fig. A-2. The linear control surface

التحكم في محرك التيار المستمر باستخدام وحدة تحكم Fuzzy التناسبي التكاملي + التفاضلي معتمدة علي الخوارزميات الجينية

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الملخص:

تقدم هذه المقالة طريقة تحكم لمحرك تيار مستمر باستخدام وحدة تحكم Fuzzy التناسبي التكاملي + التفاضلي مبنية علي الخوارزميات الجينية. طريقة التحكم هذه مناسبة عندما تكون هناك إمكانية تطبيق وحدة تحكم التناسبي التكاملي التفاضلي . والفكرة وراء هذا المتحكم هي ضبط معاملات التحكم التقليدية (التناسبي التكاملي التفاضلي) باستخدام الخوارزميات الجينية ثم حساب ما يكافئها في مجال Fuzzy . وقد استخدمت المعاملات المضبوطة هذه كقيم أولية لمعاملات وحدة التحكم Fuzzy التناسبي التكاملي + التفاضلي. وحدة التحكم الجديدة المقترحة، Fuzzy التناسبي التكاملي + التفاضلي، تم تطبيقها للتحكم في سرعة محرك تيار مستمر على مدى واسع من سرعات التشغيل. وعلاوة على ذلك، فإن المتحكم المقترح نجح في تحسين أداء النظام حتى مع تغيير معاملات النظام.